# Neural Networks for Classification Convolutional Networks for Image Classification

Joseph Le Roux

18/10/25

Joseph Le Roux Neural Networks for Classification 18/10/25 1/23

# Outline

- Convolutions
- For Image Processing
- For Feature Extraction

Joseph Le Roux Neural Networks for Classification 18/10/25 2/23

Notes	
Notes	
	—

### Convolutions

#### Discrete Convolution between two vectors

Convolution of filter a over input v

$$f = a * v$$
 such that  $f_n = \sum_{m=-\infty}^{+\infty} a_m v_{n-m}$ 

Can be difficult to read. Let's rewrite it:

$$f_n = \sum_{p,q \text{ s.t. } p+q=n} a_p v_q$$

Example 
$$a = [1, 2, 3]$$
 and  $v = [4, 5, 6, 7]$  give  $f = [4, 13, 28, 34, 32, 21]$ 

$$f_0 = a_0 v_0 = 4$$

$$f_1 = a_0 v_1 + a_1 v_0 = 13$$

$$f_2 = a_0 v_2 + a_1 v_1 + a_2 v_0 = 28$$

print(np.convolve([1,2,3], [4,5,6,7]))

$$f_3 = a_0 v_3 + a_1 v_2 + a_2 v_1 = 34$$

[ 4 13 28 34 32 21]

$$f_4 = a_1 v_3 + a_2 v_2 = 32$$

$$f_5 = a_2 v_3 = 21$$

Joseph Le Roux

Neural Networks for Classification

18/10/25

/ 23

### Convolution Layers in Pytorch

In Pytorch this was called a 1D convolution.

### Let's code this with PyTorch API

```
import torch
```

tensor([ 4., 13., 28., 34., 32., 21.])

Joseph Le Roux Neural Networks for Classification 18/10/25 5/23

Notes			
Votes			
·		·	·

### A Little Picture

Here be drawing...

Joseph Le Roux

Neural Networks for Classification

18/10/25

# Convolutions for Images (1)

(we forget about reversing filters from now on...)

# Why convolution?

- we want to represent a linear transformation of a patch
- need to fix a small discrepancy between the mathematical convolution and the computer vision convolution.

### Instead of vectors, matrices

- = our image is a matrix M, i.e. a  $32\times32$ , where each point is value between 0 (black) and 1 (white) (we'll change that later)
- filter A is a matrix (usually square)  $k \times k$ , (k = 3, 5... odd)

Joseph Le Roux Neural Networks for Classification 18/10/25 8/2:

lotes			
lotes			

# Convolutions for Images (2)

if we adapt the previous formula, the output is a matrix f where:

$$f_{ij} = \sum_{n=-\infty}^{\infty} \sum_{m=-\infty}^{\infty} A_{nm} M_{i-n,j-m}$$

 $\boldsymbol{p}$  little drawing shows this is not exactly what we want

let's have the filter "centered" around position ij

let's define  $p = \frac{k}{2}$  (rounded down)

$$f_{ij} = \sum_{n=-\infty}^{\infty} \sum_{m=-\infty}^{\infty} A_{p+n,p+m} M_{i-n,j-m}$$

- now, little drawing shows this is exactly what we want
- really?

Joseph Le Roux

Neural Networks for Classification

18/10/25

9 / 23

# Convolutions for Images (3)

### More realistically

images are not matrices

- each point can have several pieces of information, called channels, encoded as vectors
- for instance:
  - 3 channels for RGB coding (red/green/blue)
  - either integer between 0 and 255, or
  - float between 0 and 1
- Images are encoded as 3d tensors:  $C \times W \times H$  with C = 3
- Bias term b : compute affine functions instead of linear

$$f_{ij} = b + \sum_{c=0}^{C-1} \sum_{n=-\infty}^{\infty} \sum_{m=-\infty}^{\infty} A_{c,p+n,p+m} M_{c,i-n,j-m}$$

Joseph Le Roux Neural Networks for Classification 18/10/25 10

Votes			
Votes			
Notes			
Votes			
Notes			
Notes			
Votes			
Notes			

# Convolutions for Images (4)

What can we do with convolutions? Alter each pixel!

### Example Average (blurring effect)

First, load a picture

```
import torch
from torchvision import io
import matplotlib.pyplot as plt
img = io.read_image("../static/IMG_20220726_161509.jpg")
fig = plt.figure(figsize=(img.size(1)/ 150,img.size(2) / 150))
plt.imshow(img.permute(1,2,0))
```



Joseph Le Roux

Neural Networks for Classification

18/10/25

# Convolutions for Images (5)

# Average (blurring effect)

Second, apply an average convolution

```
ks, n_ch = 20,3 # kernel size (patch size) and number of channels (RGB)
conv = torch.nn.Conv2d(n_ch, n_ch, ks, padding=ks-n_ch + 1, bias=False) #no bias
conv.weight.requires_grad=False #so we can replace values manually
print(conv.weight.size()) #(3,3,20,20)
conv.weight[:,:,:,:] = torch.zeros(n_ch,n_ch,ks,ks) #reset all values to zero
patch = torch.ones(ks,ks) / (ks*ks) # uniform dist.
conv.weight[0][0] = patch # for R channel
conv.weight[1][1] = patch # for G channel
conv.weight[2][2] = patch # for B channel
img = img.to(torch.float)/256 # all values between 0 and 1
blurred = conv(img)
io.write_jpeg((256*blurred).to(torch.uint8), "blurred.jpg", 100)
```

Joseph Le Roux Neural Networks for Classification

Notes			
Notes			

# Convolutions for Images (6)

### Average (blurring effect)



Joseph Le Roux

Neural Networks for Classification

18/10/25

13 / 23

# Convolutions for Images (7)

# Sharpening (edge detection)

```
ks, n_ch = 20,3 # kernel size (patch size) and number of channels (RGB)
conv = torch.nn.Conv2d(n_ch, n_ch, ks, padding=ks-n_ch + 1, bias=False) #no bias
conv.weight.requires_grad=False #so we can replace values manually
print(conv.weight.size()) #(3,3,20,20)
conv.weight[:,:,:,:] = torch.zeros(n_ch,n_ch,ks,ks) #reset all values to zero
ks, n_ch = 3, 3  # kernel size (patch size) and number of channels (RGB)
conv = torch.nn.Conv2d(n_ch, n_ch, ks, padding=ks - n_ch + 1, bias=False) # no bias
conv.weight.requires_grad = False # so we can replace values manually
print(conv.weight.size()) # (3,3,3,3)
conv.weight[:, :, :, :] = torch.zeros(n_ch, n_ch, ks, ks) # reset all values to zero
[0, -1, 0]]) / 4)
conv.weight[0][0] = patch # for R channel
conv.weight[1][1] = patch # for G channel
conv.weight[2][2] = patch # for B channel
img = img.to(torch.float)/256  # all values between 0 and 1
sharpened = conv(img)
io.write_jpeg((256*sharpened).to(torch.uint8), "sharpened.jpg", 100)
```

Joseph Le Roux Neural Networks for Classification 18/10/25 14/25

Votes			
Notes			
Notes			
Votes			
Notes			
Jotes			
Notes			
Votes			
Jotes			
Jotes			
Notes			
Jotes			
lotes			
Notes			

# Convolutions for Images (8)

### Average (blurring effect)



Fun... but that is not what we will use convolutions for :(

Joseph Le Roux

Neural Networks for Classification

18/10/25

15 / 23

# Convolutions for computing representations

- channels represent information about points (samples) in the image
- at the beginning, we only have information about pixel color (RGB)
- we want:
  - 1. incorporate information about neighbours
  - 2. move from information about points to information about zones/areas
  - 3. bigger and bigger areas until we have information about the entire image and make a prediction
- steps 1 and 2 will be repeated
- step 3 will be a MLP from the final image information

### To sum up:

- step 1 realized by convolution
- step 2 realized by pooling (seen next)
- step 3 realized by MLP

Joseph Le Roux Neural Networks for Classification 18/10/25 17/23

Notes		
Notes		

# Convolutions to extract information about neighbours (1)

#### Compute several filters for each position

```
ks, n_in_ch, n_out_ch = 5,3,12 # kernel size, input channels, output channels conv = torch.nn.Conv2d(n_in_ch, n_out_ch, ks) # compute n_out_ch filters print(conv.weight.size(), conv.bias.size()) # (12,3,5,5), (12)

print(img.size()) # (3, 640, 480) each pixel has 3 informations img_w_neighbour_info= conv(img) print(img_w_neighbour_info)# # (12, 636, 476) whaaaat!!!
```

- We have the right number of output channels, but the image is shrunk
- Convolutions are centered, so extreme image points are ignored

Joseph Le Roux

Neural Networks for Classification

18/10/25

18 / 23

# Convolutions to extract information about neighbours (2)

### Size of the resulting matrix

## How many consecutive k positions in a vector of size n

- n-k+1 (draw picture if need be)
- this means that each convolution loses some positions

### Padding to control the output size

use padding to add fake positions around image (zero by default)

```
ks, n_in_ch, n_out_ch = 5,3,12
conv = torch.nn.Conv2d(n_in_ch, n_out_ch, ks, padding=2)
print(img_size()) # (3, 640, 480) each pixel has 3 informations
img_w_neighbour_info= conv(img)
print(img_w_neighbour_info) # # (12, 640, 480)
```

seph Le Roux Neural Networks for Classification

18/10/2

25

19/23

Notes		
Notes		

# Pooling

#### With convolutions

- represent each point by taking information from neighbourhood
- represent the same number of points (approx, with padding)
- change only de number of channels (aka depth)
- how do we represent zones of the images instead of points?

### Pooling

- create a summary of zone
- do not change the depth
- change the size (aka the spatial representation)

Joseph Le Roux

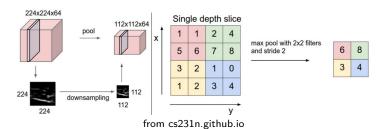
Neural Networks for Classification

18/10/25

20 / 23

# Example: Max-Pooling

Implement pooling by returning for each channel the maximum value on a patch.



print(img\_w\_neighbour\_info)# just a reminder (12, 640, 480)
mp = torch.nn.MaxPool2D(2)
img\_small = mp(img\_w\_neighbour\_info)
print(img\_small.size()) # 12,320,240

### Other Pooling Methods, Instead of max use:

- min
- average
- ...

Joseph Le Roux Neural Networks for Classification 18/10/25

Notes		
Notes		

# Putting it all together

```
class ConvNet1(torch.nn.Module):
 def __init__(self,):
   super().__init__()
   self.c1 = torch.nn.Conv2d(1, 10, 3, padding=1)
   self.m1 = torch.nn.MaxPool2d(2)
   self.c2 = torch.nn.Conv2d(10, 20, 5)
   self.m2 = torch.nn.MaxPool2d(2)
   self.c3 = torch.nn.Conv2d(20, 40, 3)
   self.m3 = torch.nn.MaxPool2d(3)
   self.fc = MLP(40, [30, 20], NB_CLASSES, torch.nn.ReLU)
  def forward(self,x):
   #print(x.size())
   x = self.c1(x)
   x = self.m1(x)
   x = self.c2(x)
   x = self.m2(x)
   x = self.c3(x)
   x = self.m3(x)
   x = self.fc(x)
   return x
```

Joseph Le Roux

Neural Networks for Classification

18/10/25

22 / 23

# Things we did not cover

# Dropout

Randomly set neurons to zero during training, avoid overfitting, make the learned model more robust

#### Normalization

Like in image processing, it is often a good idea to normalize input (center values around zero, with variance  $1\dots$ )

### Transformers

Can we develop an architecture where the kernel<sub>size</sub> can be as large as the size of the picture?

#### Generation

Can we use convolutions to generate image instead of classifying them?

Joseph Le Roux Neural Networks for Classification 18/10/25 23/23

lotes			
Notes			
Votes			
Notes			
Notes			
Votes			
Votes			
Notes			
Notes			
Notes			
Votes			
Votes			
Votes			
Notes			
Notes			
Notes			
Votes			
Votes			
Votes			